Possession Sketches: Mapping NBA Strategies

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Abstract

We present Possession Sketches, a new machine learning method for organizing and exploring a database of basketball player-tracks. Our method organizes basketball possessions by offensive structure. We first develop a model for populating a dictionary of short, repeated, and spatially registered actions. Each action corresponds to an interpretable type of player movement. We examine statistical patterns in these actions, and show how they can be used to describe individual player behavior. Leveraging this “vocabulary” of actions, we develop a hierarchical model that describes interactions between players. Our approach draws on the topic-modeling literature, extending Latent Dirichlet Allocation (LDA) through a novel representation of player movement data which uses techniques common in animation and video game design. We show that our model is able to group together possessions with similar offensive structure, allowing efficient search and exploration of the entire database of player-tracking data. We show that our model finds repeated offensive structure in teams (e.g. strategy), providing a much more sophisticated, yet interpretable lens into basketball player-tracking data.

1 Introduction

Player-tracking data present a unique challenge for basketball analytics. It is widely believed that a windfall of quantitative insight is hidden in these data, in spatiotemporal patterns that coaches and analysts typically process with human intuition. While there has been work toward quantifying player ability [6], possession value [4, 3], and play classification based on small sets of labeled plays [13], methods for automatically organizing, summarizing, and interpreting basketball possessions have yet to be fully developed.

As an example, consider the following use case for defensive scouting: an analyst is tasked with finding all possessions in which James Harden drives to the basket and passes the ball to a teammate for a right corner three-point attempt. Simple engineering solutions for this scenario are easy to imagine: first sub-select Rockets possessions with a right corner three-point attempt and then look for passes from Harden that originate in the paint. However, adding search criteria quickly renders this ad hoc solution intractable: find sequences where Harden uses a high screen before driving to the basket and then passes to the corner for a three-point attempt; find sequences where Harden uses a high screen, drives to the basket, passes to the corner and that teammate drives to the basket; find sequences where any Rocket uses a high screen, drives to the basket, etc. The landscape of relevant basketball scenarios is far too vast and complex for ad hoc search solutions.

Furthermore, this type of sequential query is only one approach to gaining insight from player-tracking data. We can imagine starting a research project by simply asking — what leads to a corner three? What sort of patterns are employed by different offenses in order to get an open three-point attempt? What sorts of actions do specific players tend to do in order to generate an open three-point attempt? Existing methodology falls short of supporting this kind of exploratory analysis with player-tracking data.
In this work, we bridge this gap by formulating a novel machine learning method to describe an entire database of player-tracks. Our method uncovers characteristic patterns of offense in a way that is searchable and interpretable. We first describe individual player’s actions by building a data-driven dictionary of action templates derived from a statistical model. We then construct a model of possessions that describes patterns in these action templates — common co-occurrences that create a signature of offensive strategy. For each play, this yields a possession sketch, a concise summary of the offense’s actions in a basketball possession. We model this structure at multiple levels — in dynamic actions taken by individual players, as well as collective actions present in each possession.

Importantly, we construct our model out of interpretable pieces — each action template can be interpreted as a type of on- or off-ball cut. Further, pairs of actions are also interpretable — some correspond to on-and off-ball screens, others correspond to drives and passes to various wings. Our use of probabilistic graphical models on an interpretable representation of the data allows for easier-to-understand model output and inferences than recent deep learning approaches [13].

In the following section we describe the components of our method that generate action templates and possession sketches. After describing our method, we explore the structure it reveals by looking at three of the different organizational tools it makes possible:

- **team possession maps**: low-dimensional visualization of all of the offensive possessions of a team — exploring this map reveals different set calls used by a team.
- **shot possession maps**: low-dimensional visualization of possessions that led to a particular type of shot — we examine the different types of actions that lead to corner threes.
- **possession basis**: common and repeated actions discovered by the model — this establishes the types of player interaction that make up the “vocabulary” of a basketball possession.

By integrating machine learning methods, statistics, and visualization, this work shows that we can organize and systematically explore NBA possessions, allowing us to derive useful basketball intelligence from the NBA’s vast and growing store of player-tracking data.

## 2 Methods

This section details the machine learning model we construct to recognize patterns at two resolutions: spatiotemporal patterns in individual player trajectories (action templates), and co-occurrence of actions in each possession (possession sketches).

Before we go into further detail, the overall procedure behind our method can be decomposed into the following steps:

- **Segmentation**: We cut possession-length (e.g. 5-24 second) player trajectories into shorter, more manageable segments (e.g. .6-8 second) based on moments of sustained low-velocity.
- **Learning action templates**: We formulate a novel statistical clustering algorithm to learn which action is represented by each short segment.
- **Possession modeling**: We represent each possession as a “bag” of pair-actions, and fit a possession-level hierarchical model inspired by the document modeling and natural language processing literature.

The following subsections describe the process of applying the above steps to a large data set of basketball player-tracks.

### 2.1 Data and preprocessing

We analyze a database of player-tracks from the 2014-2015 season of the NBA. The data are organized into over $N = 190,000$ possessions (and possessions into quarters and games). For each possession (indexed by $n$), we model the trajectories of players on offense. For each player (indexed by $j$) in possession $n$, we cut their trajectory (denoted $x_j^{(n)}$) into short segments at locations of sustained low-velocity.
To do this, we first detect moments of low velocity by inspecting the smoothed first difference of the trajectory. At sustained moments of low velocity (> 0.25 seconds below a threshold of 1 foot per second), we cut the possession, resulting in a collection of shorter segments. Figure 1 depicts four example trajectories, cut into various number of segments.

We refer to these shorter trajectory segments as $x_{(n)}^{j_1}, \ldots, x_{(n)}^{j_S}$, where it is understood that the number of segments, $S$, varies for each possession-player pair. The resulting short segments are on average 2.25 seconds (the interior 95 percentiles range from 0.6 to 7.96 seconds). Applying this preprocessing step to the full 2014-2015 regular season creates a data set of roughly 4.5 million segment observations.

### 2.2 Action Templates: Segment Clustering

Our method assumes that each short trajectory segment represents some discrete action, and each player performs a series of actions throughout the course of a possession. For instance, a player might (i) make a cut along the baseline and then (ii) camp out in the corner. Alternatively, a player can (i) make a cut along the 3-point line, (ii) stand at the break, then (iii) cut toward the basket. In order to decompose a player’s trajectory into a set of actions, we must first infer a meaningful set of actions that all players share. We use a data-driven approach to infer this set of actions, each action’s structure, and the action label for each trajectory segment.

To accomplish this, we construct a probabilistic clustering algorithm tailored for functional data (i.e. continuous trajectories). Our model posits that each trajectory segment represents one of $V$ discrete actions, where each action is characterized by a template. Each template can be thought of as a cluster center — each observed trajectory segment is centered around a template with some deviation. We specify each template as a Bezier curve – a tool commonly used to model movement in the computer graphics community – which specifies a function $B(t)$ that maps time to a two-dimensional point, $B : [0, 1] \mapsto \mathbb{R}^2$. This maps out a dynamic curve through space, which describes the movement of each action. See the appendix for technical details.

Figure 2 depicts a sampling of learned templates resulting from fitting a mixture of $V = 250$ Bezier
Figure 2: A sampling of action templates. Our method automatically builds a taxonomy of commonly repeated movements shared among all players (i.e. actions). In each column, the top plot depicts the spatial trajectory for a single action template. The light blue lines are real segment trajectories that fall in that cluster. Below each action plot is a histogram of segment lengths (in seconds) for all segments that fall into that cluster — some actions are shorter or longer (on average) than others. For a more dynamic picture of an action template, please view this animated figure: https://youtu.be/-a6_Ot6etmk

curves to the processed trajectory segments. The output of this model allows us to succinctly represent each trajectory segment as a single integer, \( v = 1, \ldots, 250 \). We view these actions as a kind of vocabulary — each possession combines words in the vocabulary to describe structured interactions that characterize the possession. Following this thread, we turn to statistical methods originally devised for modeling documents, and adapt them to basketball sequences.

2.3 Possession Model

Offensive possessions are highly structured. When James Harden drives toward the basket, drawing defender attention, his teammates are not distributed randomly on the floor — it is likely that at least one teammate is in the corner waiting for a pass; it is likely that other teammates vacate the paint, and begin jockeying for rebounding position. The structure of an offensive possession is created by the individual actions that each player performs throughout the possession. Which actions tend to simultaneously co-occur? Which actions tend to precede or follow other actions? Our possession model seeks to answer these questions by first observing that these actions are a lot like words. Words are interwoven sequentially to express a coherent idea; player actions are interwoven sequentially to implement a coherent strategy. We run with this analogy by adapting topic models [1] to describe sequences of actions in basketball possessions.

We use Latent Dirichlet Allocation (LDA) [2], a topic model for unsupervised structure discovery in a corpus of text documents. LDA is a latent factor model, similar to factor analysis or principal components analysis. In document modeling, LDA describes each document as a mixture of topics, where each topic is a distribution over the entire vocabulary of words. As a concrete example, LDA applied to a corpus of Science articles finds topics corresponding to cancer (e.g. probable words are “tumor”, “cell”, “cancer”, etc.), and neuroscience (“synaptic”, “neurons”, “hippocampal”, etc.), among many others (see [8, 1]).

In our application, rather than topics, we represent each possession as a mixture of strategies, where
Figure 3: The “bag of words” construction of each possession. Each “word” represents two actions that occur simultaneously throughout the course of the possession, where actions are inferred with the action template model presented in Section 2.2. In the toy example depicted, we have three players, each performing a sequence of actions (corresponding to the four colors). At each moment in time, we enumerate all unique pairs of actions. We represent the entire possession as a bag of these pair-action counts.

Each strategy is a distribution over co-occurring actions that are frequently observed in the data. We then use LDA to infer the strategies employed in each offensive possession (as well as the set of strategies themselves). LDA requires that we represent each possession as a “bag of words” — a vector where each entry corresponds to a unique word and represents the number of times that word occurs in the possession. To do this, we need to first establish a vocabulary.¹ Our first approach was to simply count the number of each action in each possession. This approach is appealing in its simplicity, and does reveal interesting structure. However, this representation ignores interactions between players and temporal structure.

In this work we use a vocabulary of pair-actions, where each “word” in the vocabulary is a unique pair of the $V$ actions, $(v_i, v_j)$ for $v_i, v_j \in \{1, \ldots, V\}$ and $v_i \neq v_j$. We then represent each possession as a “bag of simultaneous pair-actions”, mapping the “bag of words” concept from topic models to basketball interactions. For each possession, we simply count the number of times each unique pair of actions simultaneously occur. We string these counts into a single vector, which represent possession

\[ Y_{n,d} = \# \text{ times action action pair } d = (v_1, v_2) \text{ appears in possession } n. \]  

Figure 3 illustrates the construction of our pair-action vocabulary that we use to succinctly represent each possession. To incorporate ball possession information, we define each action as “with” or “without” the ball², resulting in $2 \cdot V$ total player actions. We include pair-actions that appear in at least 100 possessions, resulting in about 25,000 unique pair-actions in our vocabulary. This representation allows us to apply LDA to basketball possessions. To fit this model to the over 190,000 possessions in the season, we use a recently developed scalable Bayesian inference technique [9]. See the appendix for technical details.

This model yields a low-dimensional embedding of every NBA play that allows us to quickly assess similarities between possessions and explore the space of team offensive strategies. We can create interactive graphics (a dynamic version of Figure 5a), where each point in space represents a full possession and nearby points indicate “similar” possessions — possessions that share the same pattern of actions. The following section dives deeper into this exploration tool, and what it can afford an analyst. The topics themselves encode strategic co-occurrences of actions, and using these topics we can shed

¹In document modeling, the vocabulary is typically the vocabulary of the language itself, with minimal preprocessing. Common sequences of two or three words (bi-grams and tri-grams) are sometimes included in the vocabulary to improve the model.

²An action is considered “with” ball if the player possesses the ball for the majority of the segment.
light on the fundamental building blocks of collective action on the basketball court. Inspecting these topics can help us quantify what exactly makes a unique offense unique.

3 Analysis

In this section we explore the output of the possession level model to see which patterns are represented. We focus on the following aspects of model output

- **basketball topics**: we see which pair-actions are represented by each of the $K = 100$ topics. This tells us not only which pair-actions occur frequently, but which pair-actions co-occur in possessions, revealing fundamental patterns of basketball offenses.
- **possession sketch**: each possession is characterized as a distribution over topics (or strategies), and “similarity” between possessions can be measured using this distribution. We explore what our model describes as similar, and we empirically test this notion of similarity by measuring distances between sets of plays we previously inspected and labeled as similar.

In the following sections we explore the above concepts by visualizing and exploring possessions in ways newly afforded by our framework.

3.1 Basketball Topics

Figure 4 graphically depicts a small sampling of basketball topics (i.e. strategies) discovered by the possession model. The topics reveal which pair-actions are most common in our data set, and we do see
Figure 5: Left: map of 2014-2015 Warriors possessions, with a small set of known “weave” plays highlighted in red. The weave plays tend to cluster together in this visualization. We verify this by computing the average distance between two weave possessions and between a weave and a random Warriors possession of a similar length. This indicates that our topic-model-based representation is picking up on patterns that are able to (mostly) distinguish between semantically different plays.

patterns emerge. As a concrete example, if a particular possession “loads” onto topic 3 then that possession is more likely to include the pair-actions depicted in Figure 4d — a cut to the basket while a teammate is standing in either of the two corners. Topic 5 prominently includes possessions with a baseline cut from the right block to the left break. Note that there are many more pair-actions with significant probability than the ones depicted, and there are many more topics than we depict.

Sparsity We also notice that each possession topic vector is quite sparse — on average only 8 of the 100 entries are non-zero. This is expected and desired behavior — each possession can only include a small number of offensive patterns from the wide array of available tactics.

3.2 Possession Map Exploration

Each possession has an associated possession sketch — a per-topic vector that describes how much of each of the basketball topics (a subset illustrated in Figure 4) are featured in that possession. We can use these possession sketches to reason about large sets of basketball possessions. In this section we select the offensive possessions of the 2014-2015 Golden State Warriors (over 6,000 possessions). With each possession succinctly described by a (sparse) 100-dimensional topic vector, we use the dimensionality reduction technique t-SNE [10] to visualize these vectors in 2-dimensions. This method finds a 2-dimensional representation of each 100-dimensional vector such that the distance in 2-d is similar to the distance in 100-d (emphasizing the preservation of local distances).4 Figure 5 visualizes all Warriors possessions in 2014-2015.

We test the notion of “similarity” in topic space by examining a group of hand-labeled set plays, a “weave play”. We animate two examples of the weave play in this animated figure: https://youtu.be/KRDsTLMm7FY. We hand-label 40 weave plays in the 2014-2015 season, and visualize them in the

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3. i.e. the possession sketch vector is large along the dimension corresponding to topic 3
4. For intuition, t-SNE tends to yield a visualization where locally clustered points are close in distance in the full, 100-dimensional topic space; points that are farther away from each other tend to be far, but could also be close.
t-SNE Warriors map (Figure 5a, in red). We can visually verify in Figure 5 that the possession sketch preserves this notion of similarity — weave plays tend to cluster around other weave plays.

We can further measure this clustering by comparing two distributions of possession sketch distances: (i) the distribution of distances between two weave plays, and (ii) the distribution of distances between one weave, and one non-weave play. Figure 5b illustrates these two distributions. The average distance between the known weave plays is much smaller than the average distance between weave and non-weave plays. In fact, the nearest neighbor of each weave play is most often itself a weave play, highlighting the potential of our technique to quickly find a collection of plays similar to a chosen play.

3.3 Between Team Nearest Neighbors

Our method also identifies similar possession structure between different teams. To highlight this we select a play at random, and search through the entire database of 190,000 possession sketches to find the most similar play. The resulting two possessions are compared in Figure 6. Chicago is on offense in our first possession, and Brooklyn is on offense in the nearest-neighbor possession. Examining these two possessions, we see a few salient similarities that shed light on what patterns our method is detecting: (i) the point guard brings the ball up the left side of the floor in each possession; (ii) a player sets a high screen on the left side, and the point guard curls around the screen toward the middle with the ball; (iii) through both possessions a player camps out in the weak-side corner three; (iv) the point guard attacks through the middle of the paint. The possession sketch contains this information — and we can further inspect the particular basketball topics for this possession to see how this information is summarized in our model.

3.4 Corner Threes

In this section we explore possession sketch similarity in the context of a particular type of shot — a corner three. We first sub-select the 2014-2015 data to possessions that include corner three-point shots for three teams: the Warriors, the Rockets, and the Spurs. We then apply t-SNE to visualize the sketch for each possession in Figure 7a. We immediately notice that the possession sketches that lead to corner threes overlap significantly between teams, however there are some regions of the space in which the Rockets are more likely to inhabit than the Spurs.

We examine the structure of the possession-map clusters by zooming in on two groups on the opposite side of the map. Figure 7 compares two possessions in the cluster in the left-pane to two possessions in the cluster in the right pane. An immediate difference between the two clusters is that the right pane includes a baseline cut toward the corner in which the shot is taken, whereas the left pane includes a drive into the middle, and a pass out to a player camping out in the corner. Indeed, these are two very different ways of ending up with a corner three point attempt, and our method identifies this and allows us to efficiently explore this structural variation.

4 Discussion

Related work This paper develops a framework for exploring interpretable patterns in player-tracking data — applications of this framework can enhance player evaluation and media consumption. A similar system for measuring play similarity was developed in [12], based on point-wise similarities in trajectories. Ours is a more global approach — we fit a probabilistic model to an entire season’s worth of player tracking data, directly modeling player interactions. The result is a more interpretable, succinct, and scalable decomposition of possessions.

In [4, 3], the authors propose a stochastic process model to measure the moment-by-moment expected possession value (EPV) of a basketball sequence. They handcraft a set of basketball states that

⁵Please refer to animated figures https://youtu.be/hUuPkE06xX4 (left pane) and https://youtu.be/mMcWuggrj1w (right pane).
Figure 6: An example of two very similar possessions: each sub-figure displays key frames from two possessions — one where Chicago has the ball and one where Brooklyn has the ball. These frames highlight similar features between the two possessions. For a clearer picture of “possession similarity”, please navigate to https://youtu.be/0Jlj6xekxeI to see these plays animated.

are used in the model. Our approach is more of a data-driven decomposition of basketball states that we use for exploration (but could be used within an EPV model). Other examples that develop data-driven representations from player-tracking data can be found in [11, 7, 6].

Future work and conclusion There are multiple avenues for future work. Firstly, we can improve the action template model by also inferring the number of actions using more sophisticated methods, such as Bayesian nonparametrics. The action templates should also have more temporal structure — auto-correlation and dynamic variance. Further, our possession sketch ignores much of the temporal information in each possession (a trade-off for statistical and computational efficiency). A future project could further describe the time-varying nature of possession strategies, which, for example, would allow us to identify which possessions may have started out in a “weave” set, but broke down into a different sequence.

Insight derived from player-tracking data has been promised more than delivered. We reduce this gap by devising a method that will have a profound impact on the use of player-tracking data for analysis — from summarizing situational statistics (e.g. how often did the “weave” play succeed?), to searching for similar plays (e.g. for post-game analysis), to discovering and quantifying previously unknown habits of interaction between players (e.g. for team-specific scouting).
Figure 7: Corner Three. The left pane cluster examples are similar in that they include a drive to the basket, and a pass to a teammate camping out in the corner. The right pane cluster examples are similar in that they include a baseline cut toward the corner in which the shot is taken. Please see the animated figures at https://youtu.be/hUuPkE06rX4 (left), and https://youtu.be/mMcWuqgrj1w (right).

References


A Appendix

A.1 Segment Clustering Model Details

Our clustering model specifies $V$ Bezier curve components, $B_v : [0, 1] \rightarrow \mathbb{R}^2$, each parameterized by $\theta_v \in \mathbb{R}^{P \times 2}$, where $P$ is the number of control points used to characterize the curve.\footnote{More control points allow for more flexibility in fitting shapes — we use 10 control points in our experiments}

\[ B_v(t; \theta_v) = \theta_v^T D_P(t) \quad \text{(2)} \]
\[ D_P(t) = \binom{P}{p} t^p (1-t)^{P-p} \quad \text{for } p = 0, \ldots, P - 1. \quad \text{(3)} \]

Importantly, each curve can be specified as a linear function with respect to parameters $\theta_v$, with a non-linear (but fixed) basis in time, $D_P(t)$. Bezier curves are a natural choice for these data — they are flexible, concisely parameterized, and easy to fit. The non-linear basis in time allows for a wide variety of template shapes.

The complete functional clustering model is specified as

\[ z_{j,n}^{(n)} \sim Pr(\text{action}|\pi) \quad \text{action type} \quad \text{(4)} \]
\[ x_{j,n}^{(n)} \sim \mathcal{N}(B_v(t; \theta_v), \Sigma_v) \quad \text{location at moment } t \quad \text{(5)} \]

We use maximum likelihood to learn parameters $\theta_v$, $\pi$, and $\Sigma_v$ (and therefore each action) directly from the data set of 4.5 million trajectory segments. To do so efficiently, we devise expectation maximization\textsuperscript{5} updates that exploit the linear structure of Bezier curves — each maximization step can be computed using weighted least squares. Furthermore, each expectation step can operate on each segment in parallel, allowing us to scale our method up to the 4.5 million trajectory segments. We omit the technical details of the inference procedure in this writeup for brevity.

A.2 Topic Model Details

Conceptually, LDA defines $K$ topics, $\phi_k$, each a distribution over actions. Each observed possession is characterized by some latent distribution over topics, $\pi^{(n)}$, which describes the probability that a particular topic is expressed in possession $n$. These two distributions — possession-specific proportions and global topics — determine the probability of observing any particular action in possession $n$. LDA posits the following data generating process to give rise to the matrix of counts

\[ \phi_k \sim \text{Dir}_V(\alpha_0) \text{ for } k = 1, \ldots, K \quad \text{(6)} \]
\[ \pi^{(n)} \sim \text{Dir}_K(\alpha) \text{ for } n = 1, \ldots, N \quad \text{(7)} \]
\[ Y_{n,:} \sim \text{Mult}(M_n, p = \sum_k \pi^{(n)}_k \phi_k) \quad \text{(8)} \]

where $M_n$ is the total number of actions present in possession $n$ (a fixed constant). We use statistical inference techniques to infer both the global topics, $\Phi$, and the possession-specific proportions, $\pi^{(n)}$ for all possessions. Due to the size of the dataset, we use stochastic variational inference\textsuperscript{9}, a scalable method for Bayesian inference in hierarchical models.